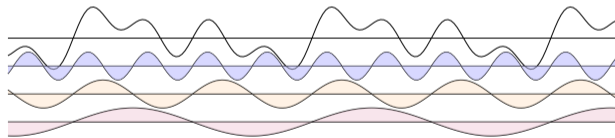


# Success and challenges of flow harmonic analysis in LHC heavy-ion physics

Jasper Parkkila, Anna Öennerstad, Dong Jo Kim

Physics Days 2021  
25. March 2021



UNIVERSITY OF JYVÄSKYLÄ



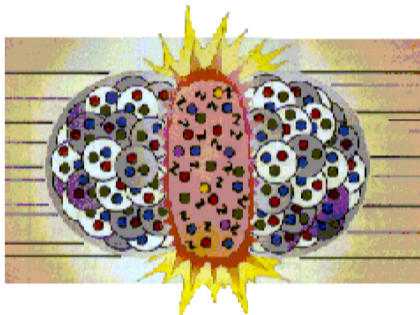
HELSINKI INSTITUTE OF PHYSICS

# Understanding Heavy-ion collisions with the collective flow

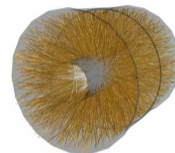
Initial geometry fluctuations

→ **Transport**  $\delta_\mu T^{\mu\nu} = 0$

→ final-state particles



Creating Quark Gluon Plasma(QGP)  
in a high energy collision



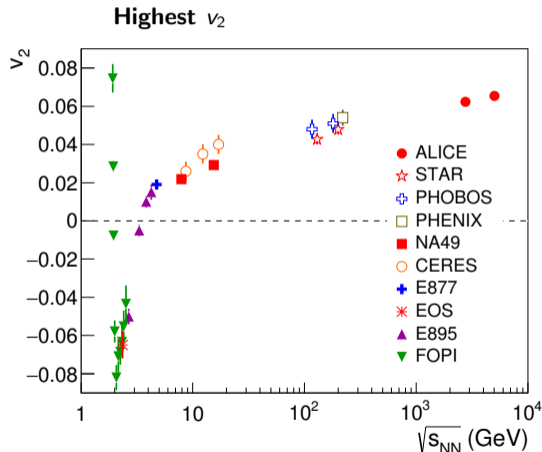
$N_{ch} \approx 1000$

$$\frac{dN}{d\phi} \propto \frac{1}{2\pi} \sum_{n=-\infty}^{\infty} \underbrace{\langle e^{in\phi} \rangle}_{V_n} e^{-in\phi}, \quad (1)$$

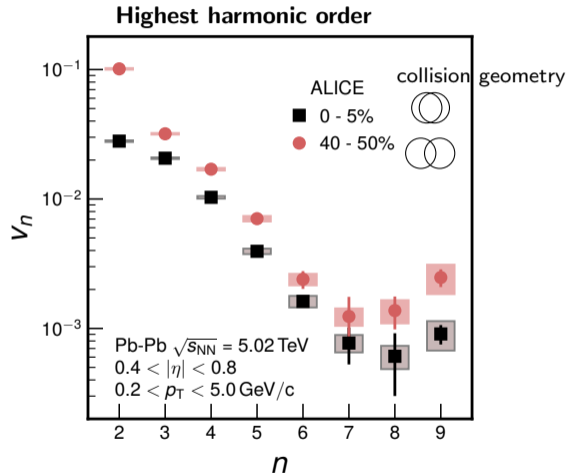
where  $V_n \equiv \langle e^{in\phi} \rangle = v_n e^{in\psi_n}$ . (experiments, theory - hydrodynamic models with  $\eta/s$ ,  $\zeta/s$ )

- Collectivity as a probe to the properties of the medium – transport properties such as  $\eta/s$ ,  $\zeta/s$

Highest  $v_2(n=2)$  and highest harmonic  $v_n(n=9)$  are measured in LHC

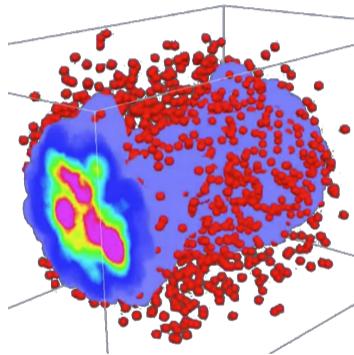


*Phys.Rev.Lett.* **105** 252302 (2010)



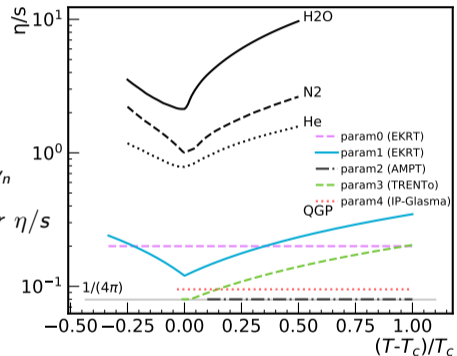
*JHEP05* 085 (2020)

Perfect quark-gluon fluid, lowest  $\eta/s$  in nature ( $\approx 1/4\pi$ )



$\uparrow$  large  $v_n$

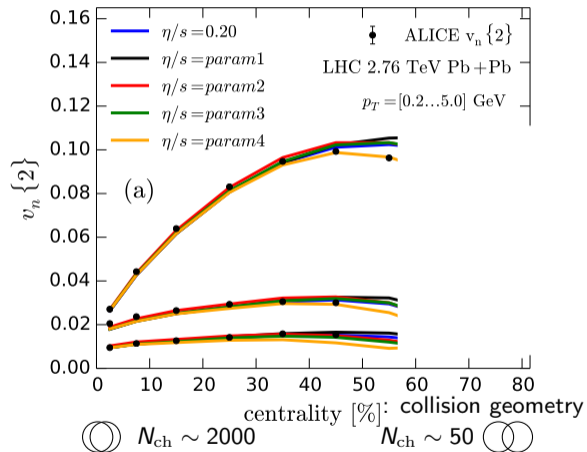
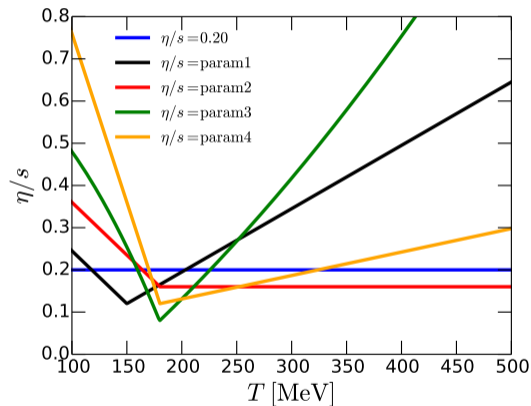
$\downarrow$  smaller  $\eta/s$



● Lower bound of the  $\eta/s$  – D. T. Son *et al.* *Phys.Rev.Lett* **94** (2005) 111601

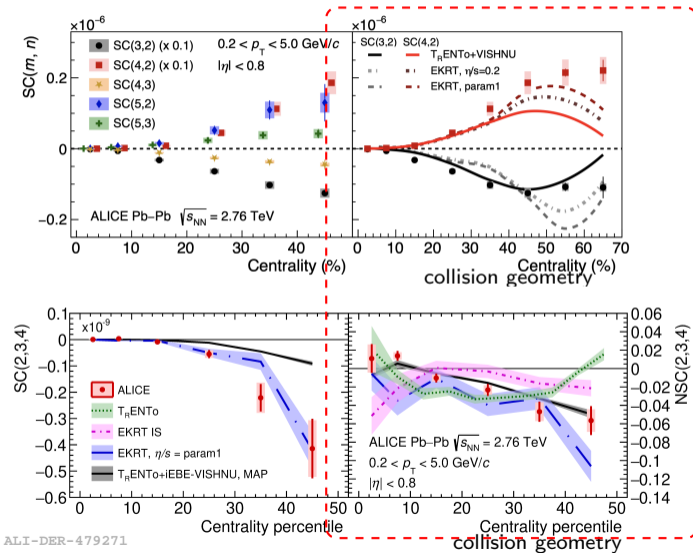
# How to constrain temperature dependence of the $\eta/s(T)$

Temperature dependent  $\eta/s(T)$  vs.  $v_n$  by H. Niemi, K.J. Eskola, R. Paatelainen, *Phys.Rev* **C93** 024907 (2016)



●  $v_n$  not sufficiently sensitive to temperature dependence.

# Measuring inner correlations of QGP, two or three harmonic correlations



$$\langle V_m V_n \rangle$$

Phys. Rev. Lett. 117 (2016) 182301

Phys. Rev. C 97 no. 2, (2018) 024906

- Temperature dependence,  $\eta/s(T)$  can be explored!
- Bonus  $\zeta/s(T)$ .

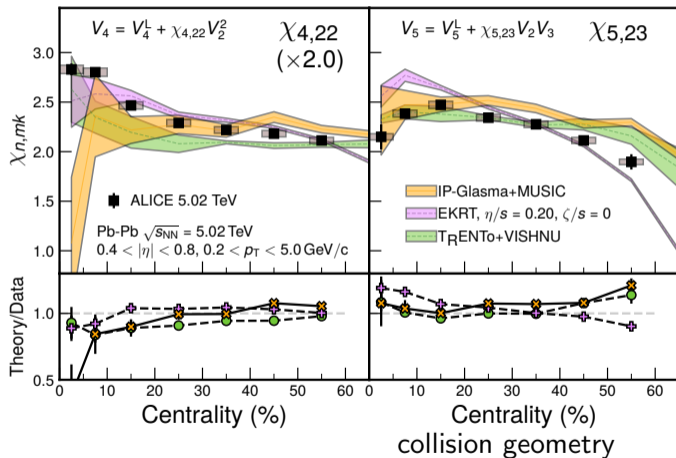
$$\langle V_k V_l V_m \rangle$$

arXiv:2101.02579, submitted to PRL

Credits to D. J Kim(Exp.) and H. Niemi(Theory)

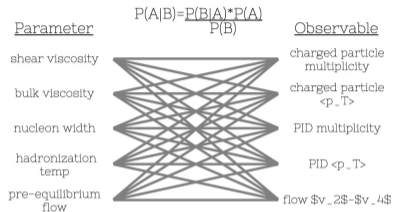
# Non-linear flow modes are measured!

Non-linear flow mode coefficients, *JHEP05 085* (2020), PhD thesis work



- higher order  $v_n$ 's are better understood!
- better sensitivity to  $\eta/s(T)$ .

# Current understanding of the medium properties

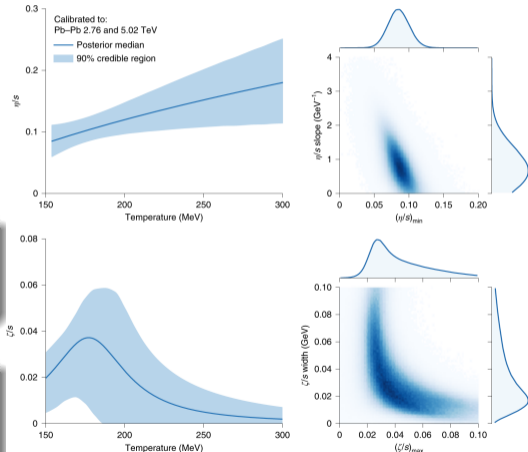


- Only low order harmonic  $v_n$  used, limited set of observables and mostly with 2.76 TeV data.
- Uncertainties need to be improved further.

Testing a single set of parameters requires  $\mathcal{O}(10^4)$  hydro events, and evaluating eight different parameters five times each requires  $5^8 \times 10^4 \approx 10^9$  hydro events.

**That's roughly  $10^5$  computer years!**

## Steffen A. Bass *et. al*, Nature Physics (2019)





# Bayesian analysis with advanced observables

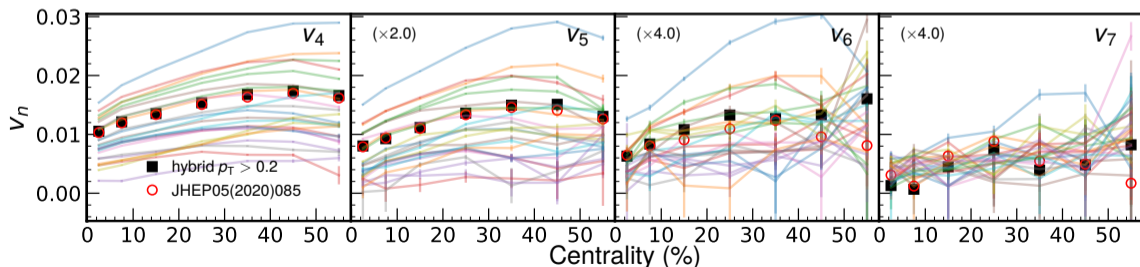
Used observables:

only with the high precision 5.02 TeV data

- Charged particle multiplicity  $N_{ch}$
- PID multiplicity (pion, Kaon and proton)
- PID  $\langle p_T \rangle$
- $v_2$  to  $v_7$  (up to  $v_9$  available)
- $\chi_{4,22}$ ,  $\chi_{5,23}$  and  $\chi_{6,m}$  (up to  $\chi_{7,223}$  available)

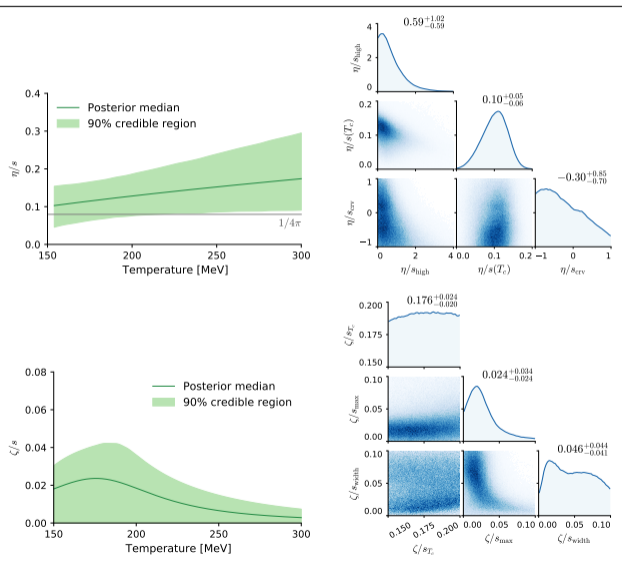
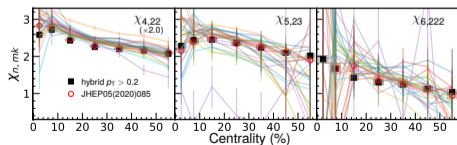
Details on productions

- CSC project 2003154 at Mahti, thanks to much improved performance.
- $\mathcal{O}(10^6)$  hydro events per one parameter point, x 100 than the previous studies.
- 900 h in 500 parameter points.



# Results with additional observables, Preliminary results

- Better constraints for  $\eta/s$ .
  - Strong correlation for higher order  $v_n$  and their non-linear response.
  - Reduced temperature dependence
- What about  $\zeta/s$ ?
  - Lower  $\zeta/s$  maximum than previously ( $\sim 30\%$ )
- Preliminary results, need to look various combinations and other parameters in detail.



# Summary

## Successes:

- QGP is nearly perfect fluid  $\eta/s \approx 1/4\pi$  based on the measurements.
- Collective flow measurements have been improved significantly in LHC, highest flow magnitude, highest harmonic orders and non-linear flow mode. → provide better constraints for the transport properties.

## Challenges:

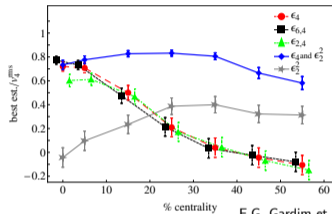
- Inclusion of High order harmonics and their non-linear responses in Bayesian analysis improved the result, showing weak temperature dependence of  $\eta/s$  and smaller  $\zeta/s$ .
- going beyond  $n > 9$  is very challenging due to high sensitivity to small data imperfections → needs further investigation for 2022- LHC runs.

# Thank you!

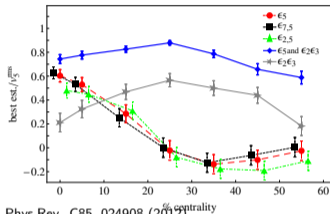
# Non-linearity of the higher order flow and cross-harmonic decomposition

- Decomposition into **linear** and **non-linear** contributions

$$v_4 e^{im\psi_4} = k \epsilon_4 e^{4i\Phi_4} + k' \epsilon_2^2 e^{4i\Phi_2}$$



$$v_5 e^{im\psi_5} = k \epsilon_5 e^{5i\Phi_5} + k' \epsilon_2 e^{2i\Phi_2} \epsilon_3 e^{3i\Phi_3}$$



$$\begin{aligned} V_4 &= V_{4L} + \chi_{4,22} V_2^2 \rightarrow v_{4,22} = \chi_{4,22} \langle |V_2|^4 \rangle^{\frac{1}{2}} \\ V_5 &= V_{5L} + \chi_{5,32} V_2 V_3 \rightarrow \dots \\ V_6 &= V_{6L} + \chi_{6,222} V_2^3 + \chi_{6,33} V_3^2 + \chi_{6,24} V_2 V_{4L} \\ &\dots \end{aligned}$$

(2)

The magnitude of the **non-linear** contribution and non-linear flow mode coefficients:

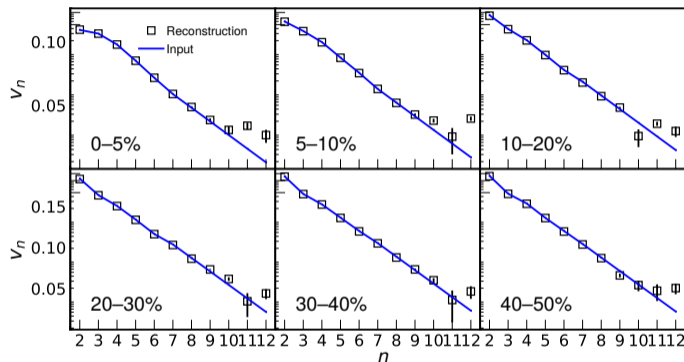
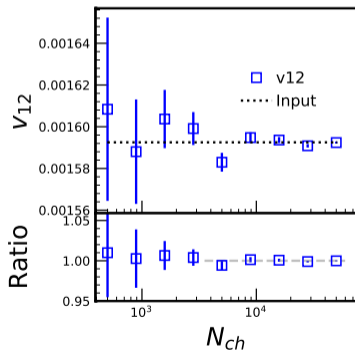
$$\begin{aligned} v_{4,22} &= \frac{\Re \langle V_4 (V_2^*)^2 \rangle}{\sqrt{\langle |V_2|^4 \rangle}} \\ &\approx \langle v_4 \cos(4\psi_4 - 4\psi_2) \rangle, \quad (3) \\ \chi_{4,22} &= \frac{v_{4,22}}{\sqrt{\langle v_2^4 \rangle}}. \end{aligned}$$

**Linear** part is extracted from the total and **non-linear** contributions:

$$\underbrace{\langle |V_{4L}|^2 \rangle^{\frac{1}{2}}}_{v_{4L}} = \left( \underbrace{\langle |V_4|^2 \rangle}_{v_4^2} - \underbrace{\chi_{4,22}^2 \langle |V_2|^4 \rangle}_{v_{4,NL}^2} \right)^{\frac{1}{2}}. \quad (4)$$

# Toward measurement of ultra-high harmonics

- Need for high precision reconstruction and correction of the  $\phi$  fine-modulations.



- Plausibility of ultra-high harmonic results. Reconstruction to be verified with ToyMC simulations.
- $0.8 < p_T < 5.0$  GeV, input = 0.00159252
- $n > 11$  needs further investigation